

COMP 3803 — Assignment 2

Due: Thursday February 14, before 11:55pm.

Assignment Policy:

- Your assignment must be submitted as one single PDF file through cuLearn.
- Late assignments will not be accepted.
- You are encouraged to collaborate on assignments, but at the level of discussion only. When writing your solutions, you must do so in your own words.
- Past experience has shown conclusively that those who do not put adequate effort into the assignments do not learn the material and have a probability near 1 of doing poorly on the exams.
- When writing your solutions, you must follow the guidelines below.
 - You must justify your answers.
 - The answers should be concise, clear and neat.
 - When presenting proofs, every step should be justified.

Question 1: Give regular expressions describing the following languages. In all cases, the alphabet is $\{0, 1\}$. Justify your answers.

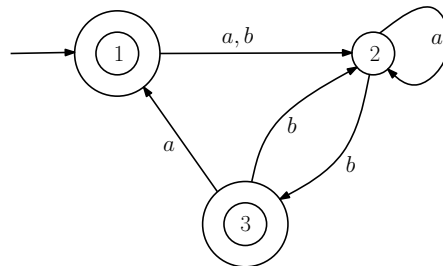
- $\{w : w \text{ contains an even number of 0s and each 0 is followed by at least one 1}\}$.
- $\{w : w \text{ contains exactly two 0s and at least two 1s}\}$.
- $\{w : \text{every odd position in } w \text{ is 1}\}$.

Question 2: Use the construction given in class to convert the regular expression

$$((0 \cup 1)(11)^* \cup 0)^*$$

to an NFA. The alphabet is $\{0, 1\}$.

Question 3: Use the construction given in class to convert the following DFA to a regular expression.



Question 4: Let R be a regular expression and let A be the language described by R . Explain how to obtain a regular expression that describes the complement \overline{A} of A . You may use any result that was proven in class and Assignment 1.

Question 5: Prove that the following languages are not regular.

1. $\{a^n b^n c^{2n} : n \geq 0\}$.
2. $\{a^{3^n} : n \geq 0\}$. (Remark: a^{3^n} is the string consisting of 3^n many a 's.)
3. $\{uvu : u \in \{a, b\}^*, u \neq \epsilon, v \in \{a, b\}^*\}$.
4. $\{a^m b^n : m \geq 0, n \geq 0, m \neq n\}$. (Using the Pumping Lemma for this one is a bit tricky. You can avoid using the Pumping Lemma by combining results about the closure under regular operations.)

Question 6: Let A be a language consisting of finitely many strings.

1. Prove that A is a regular language.
2. Let n be the maximum length of any string in A . Prove that *every* deterministic finite automaton (DFA) that accepts A has at least $n + 1$ states. (*Hint:* How is the pumping length chosen in the proof of the Pumping Lemma?)